

106 EXPONENTIAL GROWTH AND DECAY ANSWER KEY

10.6 EXPONENTIAL GROWTH AND DECAY: ANSWER KEY

STRUCTURE:

THIS DOCUMENT PROVIDES A COMPREHENSIVE ANSWER KEY FOR THE EXERCISES RELATED TO SECTION 10.6, "EXPONENTIAL GROWTH AND DECAY," TYPICALLY FOUND IN A PRECALCULUS OR INTRODUCTORY CALCULUS TEXTBOOK. THE STRUCTURE FOLLOWS THE ORDER OF PROBLEMS PRESENTED IN THE ORIGINAL TEXT (ASSUMED). EACH PROBLEM IS PRESENTED WITH ITS CORRESPONDING SOLUTION, INCLUDING DETAILED STEPS, EXPLANATIONS, AND RELEVANT FORMULAS. WHERE APPLICABLE, GRAPHICAL REPRESENTATIONS OR ALTERNATIVE SOLUTION METHODS ARE INCLUDED TO ENHANCE UNDERSTANDING. THE ANSWER KEY IS ORGANIZED INTO SECTIONS BASED ON PROBLEM TYPES (E.G., SOLVING FOR GROWTH/DECAY CONSTANTS, FINDING FUTURE VALUES, HALF-LIFE PROBLEMS, ETC.). EACH SECTION BEGINS WITH A BRIEF DESCRIPTION OF THE RELEVANT CONCEPTS AND FORMULAS USED.

DESCRIPTION:

THIS ANSWER KEY SERVES AS A VALUABLE RESOURCE FOR STUDENTS STUDYING EXPONENTIAL GROWTH AND DECAY. IT ALLOWS THEM TO CHECK THEIR WORK, IDENTIFY AREAS WHERE THEY NEED FURTHER ASSISTANCE, AND DEVELOP A DEEPER UNDERSTANDING OF THE UNDERLYING MATHEMATICAL CONCEPTS. THE DETAILED EXPLANATIONS PROVIDED GO BEYOND SIMPLY GIVING THE FINAL ANSWER; THEY OFFER INSIGHT INTO THE PROBLEM-SOLVING PROCESS, INCLUDING COMMON PITFALLS AND ALTERNATIVE APPROACHES. THE KEY IS INTENDED TO BE A LEARNING TOOL, NOT JUST A SOURCE OF ANSWERS. IT FACILITATES SELF-PACED LEARNING AND PROVIDES IMMEDIATE FEEDBACK, PROMOTING INDEPENDENT STUDY AND MASTERY OF THE SUBJECT.

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KEYWORDS: EXPONENTIAL GROWTH, EXPONENTIAL DECAY, HALF-LIFE, EXPONENTIAL FUNCTIONS, CALCULUS, PRECALCULUS, MATHEMATICS, ANSWER KEY, SOLUTIONS, PROBLEMS, GROWTH CONSTANT, DECAY CONSTANT, e , NATURAL LOGARITHM, DIFFERENTIAL EQUATIONS (IF APPLICABLE), COMPOUND INTEREST (IF APPLICABLE).

SUMMARY:

SECTION 10.6, "EXPONENTIAL GROWTH AND DECAY," EXPLORES THE MATHEMATICAL MODELS USED TO DESCRIBE PHENOMENA EXHIBITING EXPONENTIAL CHANGE. THIS ANSWER KEY PROVIDES DETAILED SOLUTIONS TO THE EXERCISES ACCOMPANYING THIS SECTION, COVERING A RANGE OF PROBLEM TYPES. STUDENTS WILL FIND COMPREHENSIVE EXPLANATIONS FOR EACH PROBLEM, INCLUDING STEP-BY-STEP SOLUTIONS, FORMULAS USED, AND, WHERE APPLICABLE, GRAPHICAL ILLUSTRATIONS. THE KEY AIMS TO CLARIFY THE CONCEPTS OF EXPONENTIAL GROWTH AND DECAY, ENABLING STUDENTS TO EFFECTIVELY APPLY THESE MODELS TO REAL-WORLD SITUATIONS AND BUILD A STRONG FOUNDATION IN EXPONENTIAL FUNCTIONS. THE DIVERSE PROBLEM SET WITHIN THE ANSWER KEY ENSURES COVERAGE OF VARIOUS APPLICATIONS, SUCH AS POPULATION GROWTH, RADIOACTIVE DECAY, AND COMPOUND INTEREST (IF COVERED IN THE ORIGINAL TEXT).

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(THE FOLLOWING SECTION WOULD CONSTITUTE THE ACTUAL 1000-WORD ANSWER KEY. DUE TO THE LENGTH CONSTRAINT OF THIS RESPONSE, I WILL PROVIDE A SAMPLE OF HOW A FEW PROBLEMS MIGHT BE PRESENTED. THIS WOULD BE REPLICATED FOR ALL PROBLEMS IN SECTION 10.6.)

SAMPLE PROBLEMS AND SOLUTIONS (FROM A HYPOTHETICAL SECTION 10.6):

SECTION 1: FINDING GROWTH/DECAY CONSTANTS

CONCEPT: THE GENERAL FORM OF AN EXPONENTIAL GROWTH/DECAY EQUATION IS $A(t) = A_0 e^{(kt)}$, WHERE $A(t)$ IS THE AMOUNT AT TIME t , A_0 IS THE INITIAL AMOUNT, k IS THE GROWTH ($k > 0$) OR DECAY ($k < 0$) CONSTANT, AND e IS THE BASE OF THE NATURAL LOGARITHM.

PROBLEM 1: A BACTERIAL CULTURE INITIALLY CONTAINS 100 BACTERIA AND GROWS AT A RATE PROPORTIONAL TO ITS SIZE. AFTER 2 HOURS, THE POPULATION HAS INCREASED TO 300. FIND THE GROWTH CONSTANT k .

SOLUTION:

1. WE HAVE $A_0 = 100$ AND $A(2) = 300$.
2. SUBSTITUTE INTO THE EQUATION: $300 = 100e^{(2k)}$
3. DIVIDE BY 100: $3 = e^{(2k)}$
4. TAKE THE NATURAL LOGARITHM OF BOTH SIDES: $\ln(3) = 2k$
5. SOLVE FOR k : $k = \ln(3)/2 \approx 0.549$ (PER HOUR)

PROBLEM 2: A RADIOACTIVE SUBSTANCE DECAYS AT A RATE PROPORTIONAL TO ITS MASS. IF THE HALF-LIFE IS 5 YEARS, FIND THE DECAY CONSTANT k .

SOLUTION:

1. HALF-LIFE MEANS $A(5) = A_0/2$.
2. SUBSTITUTE INTO THE EQUATION: $A_0/2 = A_0 e^{(5k)}$
3. DIVIDE BY A_0 : $1/2 = e^{(5k)}$
4. TAKE THE NATURAL LOGARITHM OF BOTH SIDES: $\ln(1/2) = 5k$
5. SOLVE FOR k : $k = \ln(1/2)/5 \approx -0.139$ (PER YEAR)

(THIS PATTERN WOULD CONTINUE FOR ALL PROBLEMS IN SECTION 10.6, WITH EACH PROBLEM TYPE HAVING ITS OWN INTRODUCTORY CONCEPTUAL EXPLANATION. EACH PROBLEM WOULD HAVE A DETAILED STEP-BY-STEP SOLUTION, EXPLAINING THE REASONING AND METHODOLOGY USED. WHERE APPROPRIATE, GRAPHS OR ALTERNATIVE METHODS WOULD BE INCLUDED TO ENHANCE UNDERSTANDING.)

(NOTE: THIS RESPONSE PROVIDES THE FRAMEWORK AND A SAMPLE. A COMPLETE 1000-WORD ANSWER KEY WOULD REQUIRE THE ACTUAL PROBLEMS FROM SECTION 10.6 OF A SPECIFIC TEXTBOOK TO BE SOLVED.)

DECODING 10.6 EXPONENTIAL GROWTH AND DECAY: A COMPREHENSIVE GUIDE WITH ANSWER KEY

META DESCRIPTION: MASTER EXPONENTIAL GROWTH AND DECAY WITH OUR IN-DEPTH GUIDE. WE COVER THE 10.6 PRINCIPLES, PROVIDE SOLVED EXAMPLES, AND OFFER AN ANSWER KEY TO COMMON PROBLEMS. IMPROVE YOUR MATH SKILLS AND BOOST YOUR SEARCH RANKING.

KEYWORDS: 10.6 EXPONENTIAL GROWTH AND DECAY, EXPONENTIAL GROWTH FORMULA, EXPONENTIAL DECAY FORMULA, HALF-LIFE, DOUBLING TIME, EXPONENTIAL GROWTH EXAMPLES, EXPONENTIAL DECAY EXAMPLES, SOLVED PROBLEMS, ANSWER KEY, MATH PROBLEMS, EXPONENTIAL FUNCTIONS, CALCULUS, ALGEBRA

INTRODUCTION:

EXPONENTIAL GROWTH AND DECAY ARE FUNDAMENTAL CONCEPTS IN MATHEMATICS WITH WIDE-RANGING APPLICATIONS IN VARIOUS FIELDS, INCLUDING BIOLOGY, FINANCE, AND PHYSICS. UNDERSTANDING THESE CONCEPTS IS CRUCIAL FOR ANYONE STUDYING ALGEBRA, CALCULUS, OR PURSUING STEM-RELATED CAREERS. THIS COMPREHENSIVE GUIDE DIVES DEEP INTO THE PRINCIPLES OF 10.6 EXPONENTIAL GROWTH AND DECAY, PROVIDING CLEAR EXPLANATIONS, SOLVED EXAMPLES, AND A DETAILED ANSWER KEY TO HELP YOU MASTER THIS ESSENTIAL TOPIC. WE'LL EXPLORE THE CORE FORMULAS, DELVE INTO REAL-WORLD APPLICATIONS, AND ADDRESS COMMON CHALLENGES STUDENTS FACE.

1. UNDERSTANDING EXPONENTIAL GROWTH:

EXPONENTIAL GROWTH DESCRIBES SITUATIONS WHERE A QUANTITY INCREASES AT A RATE PROPORTIONAL TO ITS CURRENT VALUE. THIS MEANS THE LARGER THE QUANTITY, THE FASTER IT GROWS. THE GENERAL FORMULA FOR EXPONENTIAL GROWTH IS:

$$A = P(1 + r)^t$$

WHERE:

A IS THE FINAL AMOUNT

P IS THE INITIAL AMOUNT (PRINCIPAL)

R IS THE GROWTH RATE (EXPRESSED AS A DECIMAL)

T IS THE TIME PERIOD

EXAMPLE 1: BACTERIAL GROWTH

A BACTERIAL COLONY STARTS WITH 100 BACTERIA AND DOUBLES EVERY HOUR. HOW MANY BACTERIA WILL THERE BE AFTER 5 HOURS?

HERE, $P = 100$, $r = 1$ (SINCE IT DOUBLES), AND $t = 5$. APPLYING THE FORMULA:

$$A = 100(1 + 1)^5 = 100(2)^5 = 3200 \text{ BACTERIA}$$

1. UNDERSTANDING EXPONENTIAL DECAY:

EXPONENTIAL DECAY IS THE OPPOSITE OF EXPONENTIAL GROWTH. IT DESCRIBES SITUATIONS WHERE A QUANTITY DECREASES AT A RATE PROPORTIONAL TO ITS CURRENT VALUE. THE GENERAL FORMULA FOR EXPONENTIAL DECAY IS:

$$A = P(1 - r)^t$$

WHERE:

A IS THE FINAL AMOUNT

P IS THE INITIAL AMOUNT

R IS THE DECAY RATE (EXPRESSED AS A DECIMAL)

T IS THE TIME PERIOD

EXAMPLE 2: RADIOACTIVE DECAY

A RADIOACTIVE SUBSTANCE HAS A HALF-LIFE OF 10 YEARS. IF WE START WITH 1000 GRAMS, HOW MUCH WILL REMAIN AFTER 30 YEARS?

HERE, $P = 1000$, $r = 0.5$ (SINCE IT'S HALF-LIFE), AND $t = 30/10 = 3$ (NUMBER OF HALF-LIVES). APPLYING THE FORMULA:

$$A = 1000(1 - 0.5)^3 = 1000(0.5)^3 = 125 \text{ GRAMS}$$

1. HALF-LIFE AND DOUBLING TIME:

HALF-LIFE: THE TIME IT TAKES FOR A QUANTITY UNDERGOING EXPONENTIAL DECAY TO REDUCE TO HALF ITS INITIAL VALUE.

DOUBLING TIME: THE TIME IT TAKES FOR A QUANTITY UNDERGOING EXPONENTIAL GROWTH TO DOUBLE ITS INITIAL VALUE.

THESE ARE CRUCIAL CONCEPTS FOR UNDERSTANDING EXPONENTIAL PROCESSES. CALCULATING HALF-LIFE OR DOUBLING TIME OFTEN INVOLVES USING LOGARITHMS, WHICH WE'LL EXPLORE FURTHER.

1. SOLVING EXPONENTIAL EQUATIONS:

MANY PROBLEMS INVOLVING EXPONENTIAL GROWTH AND DECAY REQUIRE SOLVING EXPONENTIAL EQUATIONS. THIS OFTEN INVOLVES USING LOGARITHMS TO ISOLATE THE EXPONENT.

EXAMPLE 3: FINDING THE GROWTH RATE

AN INVESTMENT OF \$1000 GROWS TO \$1500 IN 5 YEARS. WHAT IS THE ANNUAL GROWTH RATE?

$$1500 = 1000(1 + r)^5$$

$$1.5 = (1 + r)^5$$

$$(1.5)^{(1/5)} = 1 + r$$

$$r \approx 0.0845 \text{ OR } 8.45\%$$

1. APPLICATIONS OF EXPONENTIAL GROWTH AND DECAY:

THE PRINCIPLES OF EXPONENTIAL GROWTH AND DECAY ARE APPLICABLE IN A VAST ARRAY OF FIELDS:

FINANCE: COMPOUND INTEREST, LOAN AMORTIZATION, AND INVESTMENT GROWTH.

BIOLOGY: POPULATION GROWTH, BACTERIAL GROWTH, RADIOACTIVE DECAY IN BIOLOGICAL SYSTEMS.

PHYSICS: RADIOACTIVE DECAY, COOLING OF OBJECTS (NEWTON'S LAW OF COOLING).

CHEMISTRY: CHEMICAL REACTIONS, DRUG METABOLISM.

1. ADVANCED CONCEPTS:

FOR A DEEPER UNDERSTANDING, YOU CAN EXPLORE MORE ADVANCED CONCEPTS SUCH AS:

CONTINUOUS GROWTH/DECAY: USING THE FORMULA $A = Pe^{(rt)}$, WHERE 'e' IS EULER'S NUMBER (APPROXIMATELY 2.718).
DIFFERENTIAL EQUATIONS: MODELING EXPONENTIAL GROWTH AND DECAY USING DIFFERENTIAL EQUATIONS.

1. ANSWER KEY TO PRACTICE PROBLEMS:

(NOTE: PRACTICE PROBLEMS WOULD BE INCLUDED HERE. DUE TO THE WORD LIMIT, I CANNOT CREATE A FULL SET OF PRACTICE PROBLEMS AND SOLUTIONS. HOWEVER, THE EXAMPLES ABOVE SERVE AS A GOOD STARTING POINT. A COMPLETE ANSWER KEY WOULD INCLUDE STEP-BY-STEP SOLUTIONS FOR EACH PROBLEM.)

1. TROUBLESHOOTING COMMON MISTAKES:

INCORRECT UNITS: ENSURE CONSISTENT UNITS FOR TIME AND RATES.

LOGARITHM ERRORS: DOUBLE-CHECK YOUR LOGARITHM CALCULATIONS, ESPECIALLY WHEN SOLVING FOR EXPONENTS.

MISINTERPRETING THE FORMULA: UNDERSTAND THE MEANING OF EACH VARIABLE IN THE EXPONENTIAL GROWTH AND DECAY FORMULAS.

1. RESOURCES FOR FURTHER LEARNING:

NUMEROUS ONLINE RESOURCES, TEXTBOOKS, AND VIDEO TUTORIALS ARE AVAILABLE TO DEEPEN YOUR UNDERSTANDING OF EXPONENTIAL GROWTH AND DECAY. SEARCH FOR TERMS LIKE "EXPONENTIAL GROWTH AND DECAY KHAN ACADEMY," "EXPONENTIAL FUNCTIONS MIT OPENCOURSEWARE," OR "EXPONENTIAL GROWTH AND DECAY PRACTICE PROBLEMS."

1. CONCLUSION:

MASTERING EXPONENTIAL GROWTH AND DECAY IS A CRUCIAL STEP IN DEVELOPING A STRONG FOUNDATION IN MATHEMATICS AND ITS APPLICATIONS. BY UNDERSTANDING THE FUNDAMENTAL PRINCIPLES, FORMULAS, AND PROBLEM-SOLVING TECHNIQUES OUTLINED IN THIS GUIDE, YOU CAN CONFIDENTLY TACKLE VARIOUS PROBLEMS AND APPLY THIS KNOWLEDGE TO REAL-WORLD SITUATIONS. REMEMBER TO PRACTICE REGULARLY, UTILIZE AVAILABLE RESOURCES, AND SEEK HELP WHEN NEEDED. THIS COMPREHENSIVE GUIDE, ALONG WITH DEDICATED PRACTICE, WILL EQUIP YOU WITH THE SKILLS NECESSARY TO EXCEL IN THIS IMPORTANT AREA OF MATHEMATICS.

ADDITIONAL RESOURCES

106 Exponential Growth And Decay Answer Key

106 Exponential Growth And Decay Answer Key

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